

**HORIBA Scientific**

**Particle Analysis**

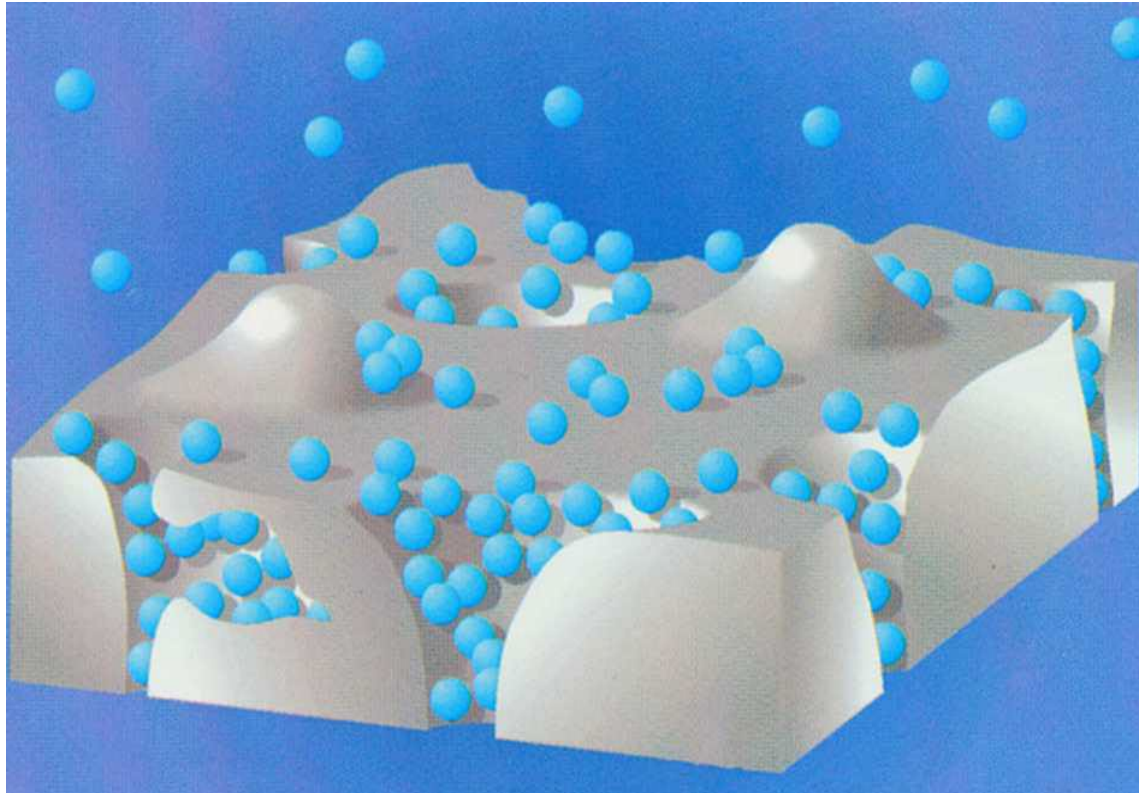
**Carl Lundstedt**

# **BET Theory and how its used to calculate surface area**

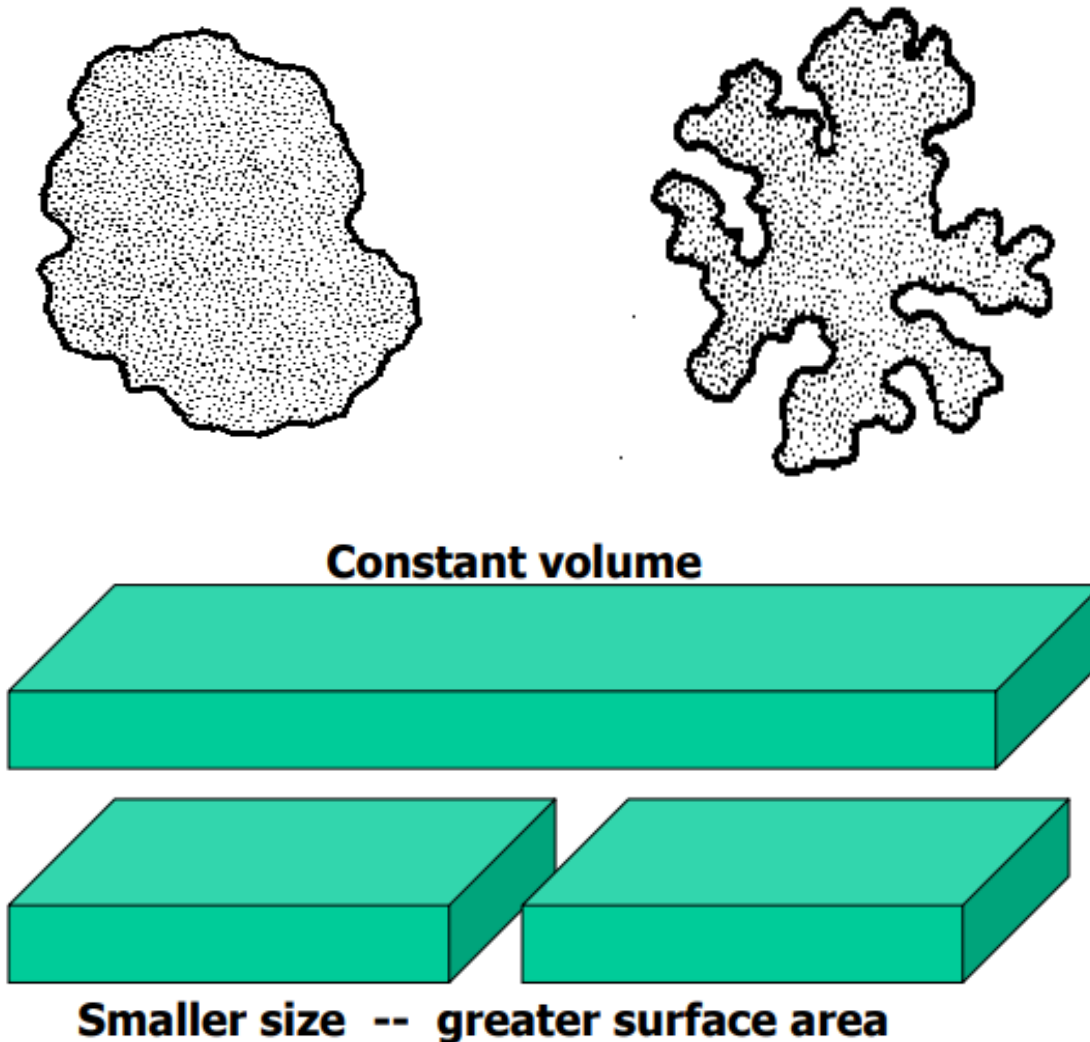
**June 25, 2019**



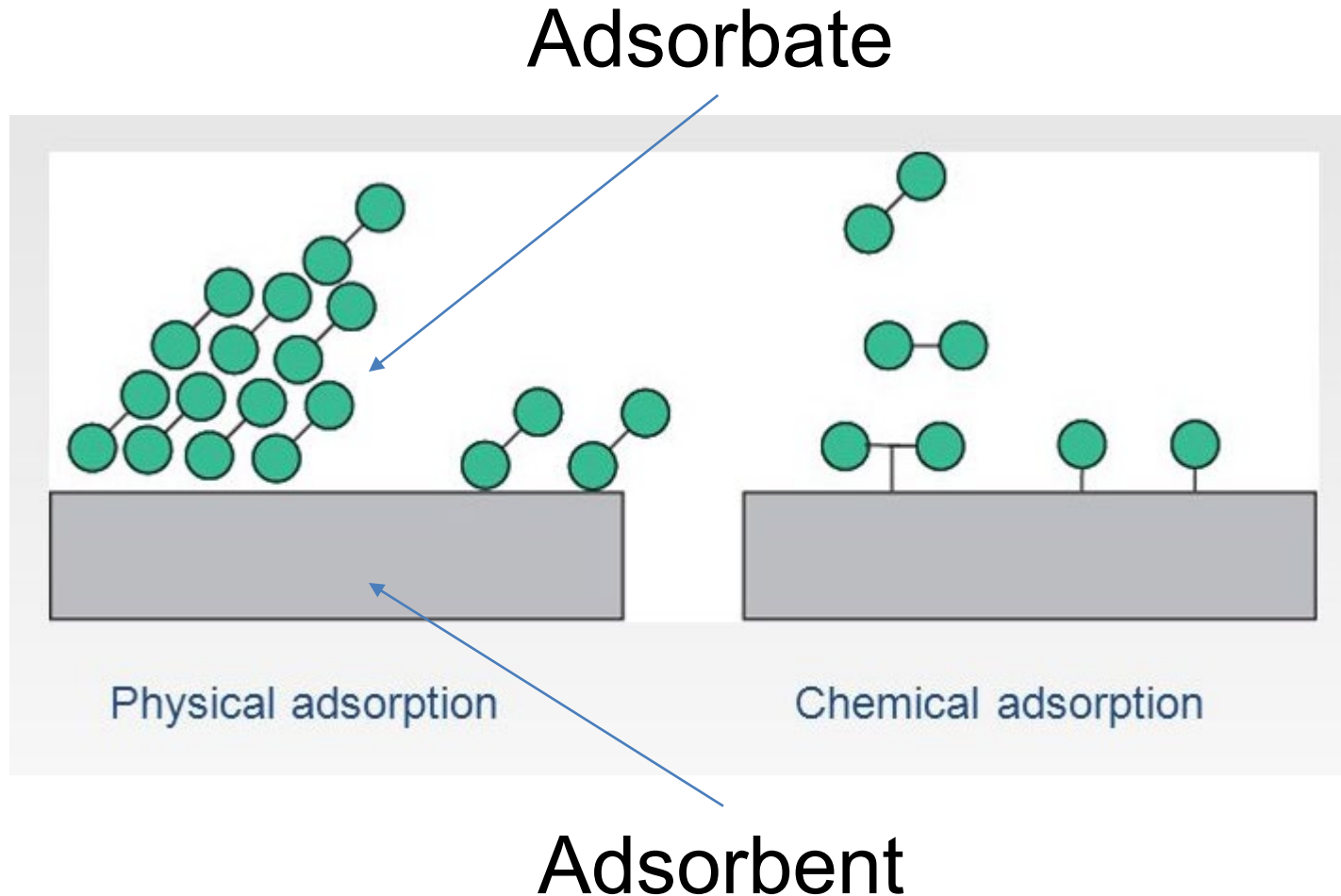
# BET Theory seeks to explain the physical adsorption of gas molecules onto solid surfaces



# Particles of similar size can vary drastically in surface area

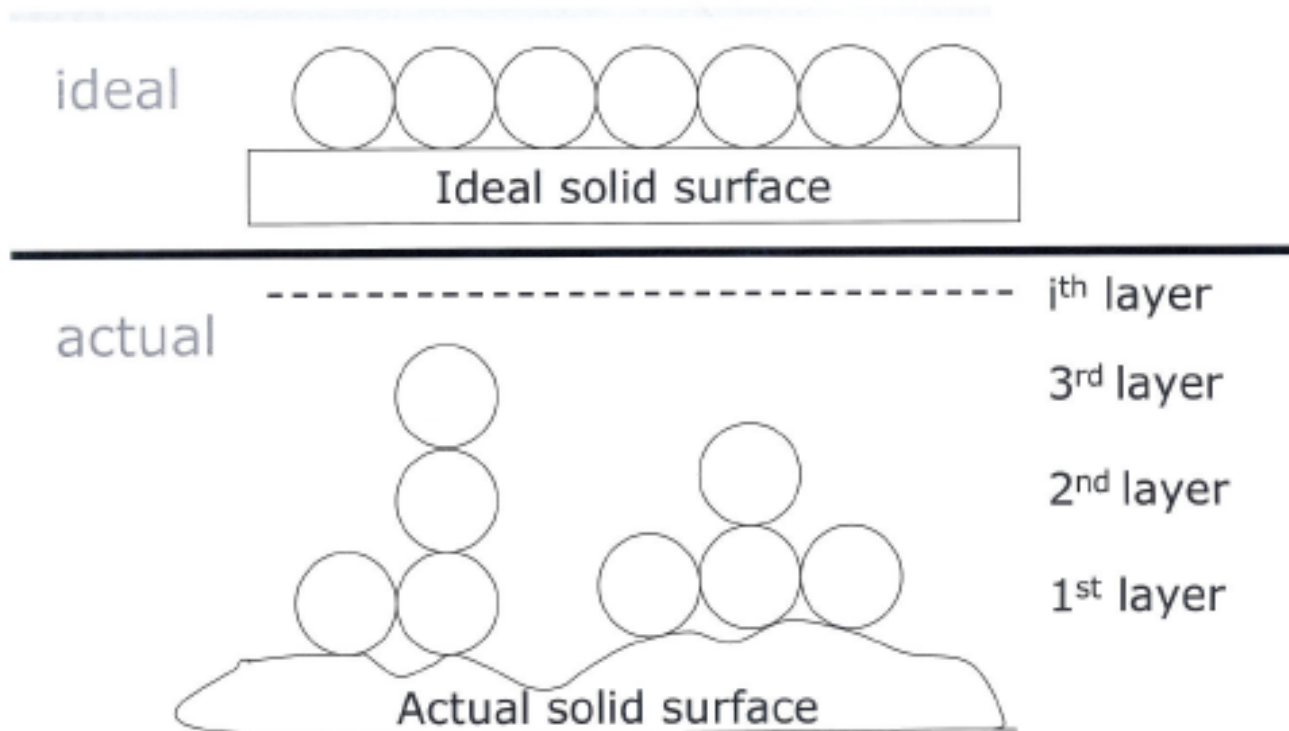


# Physical adsorption occurs due to Van der Waals forces when at low temperatures and without chemical reactions



# BET Theory extends the Langmuir theory from monolayer adsorption to multilayer adsorption

Ideal vs. actual  
physisorption behavior



# We use the BET equation to determine the monolayer absorbed gas volume ( $v_m$ )

$$\frac{1}{v[(p_0/p) - 1]} = \frac{c - 1}{v_m c} \left( \frac{p}{p_0} \right) + \frac{1}{v_m c}$$

$v$  = adsorbed gas quantity

$p_0$  = saturation pressure of adsorbate

$p$  = equilibrium pressure of adsorbate

$c$  = BET constant =  $\exp\left(\frac{E_1 - E_L}{RT}\right)$

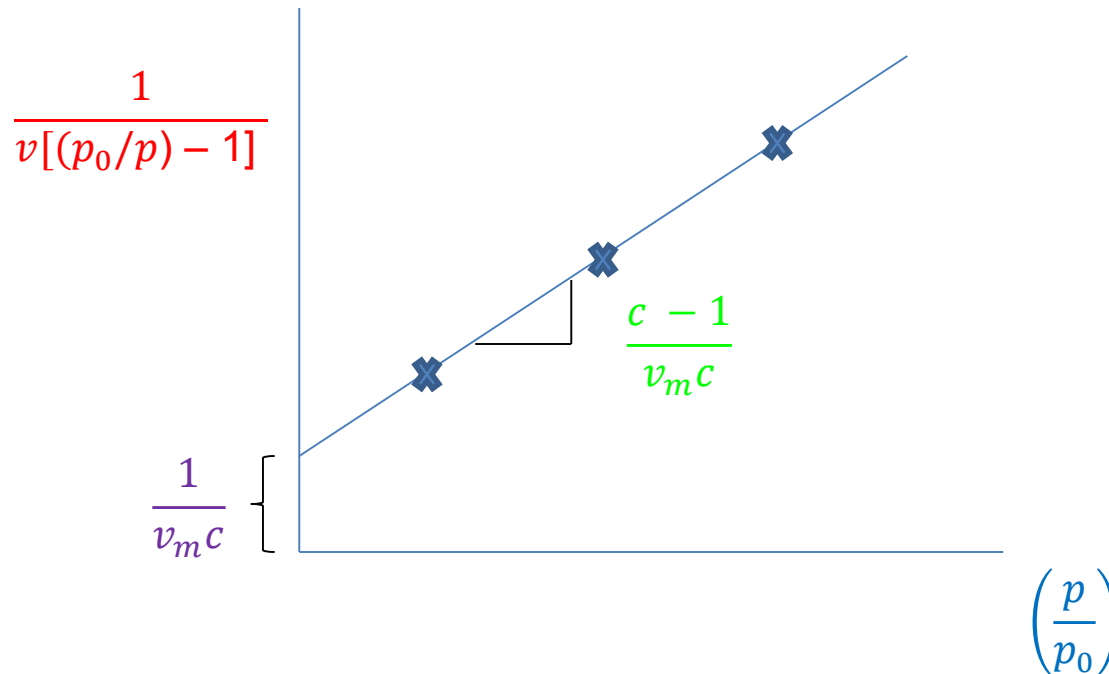
$E_1$  = heat of adsorption for the first layer

$E_L$  = heat of vaporization

# BET equation can be plotted to determine monolayer adsorbed gas quantity and the BET constant

$$\frac{1}{v[(p_0/p) - 1]} = \frac{c - 1}{v_m c} \left( \frac{p}{p_0} \right) + \frac{1}{v_m c}$$

$$y = mx + b$$



# Take numerical values for slope and intercept to solve for $v_m$ and $c$

$$\text{slope} = \frac{c - 1}{v_m c}$$

$$\text{intercept} = \frac{1}{v_m c}$$

$$v_m = \frac{1}{\text{slope} + \text{intercept}}$$

$$c = 1 + \frac{\text{slope}}{\text{intercept}}$$

**From the monolayer absorbed gas volume ( $v_m$ ), we can determine total and specific surface area**

$$S_t = \frac{v_m N s}{V}$$

$S_t$  = total surface area of sample material

$v_m$  = monolayer absorbed gas volume

$N$  = Avogadro's number =  $6.02 \times 10^{23}$  molecules/mol

$s$  = cross-sectional area of adsorbed gas molecule

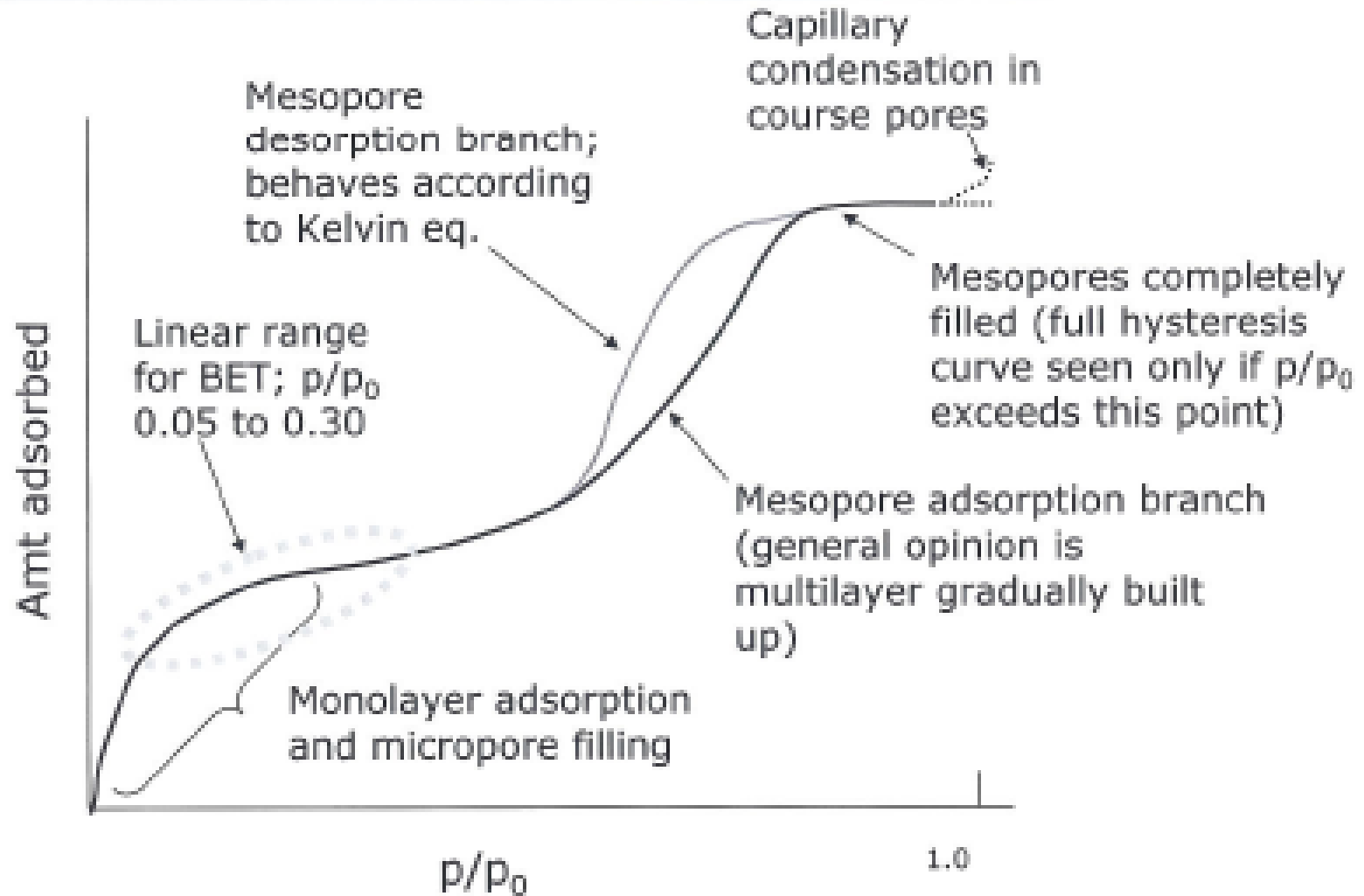
$V$  = molar volume of adsorbed gas

$$S_{BET} = \frac{S_t}{a} [=] \text{ m}^2/\text{g}$$

$S_{BET}$  = specific surface area

$a$  = mass of sample

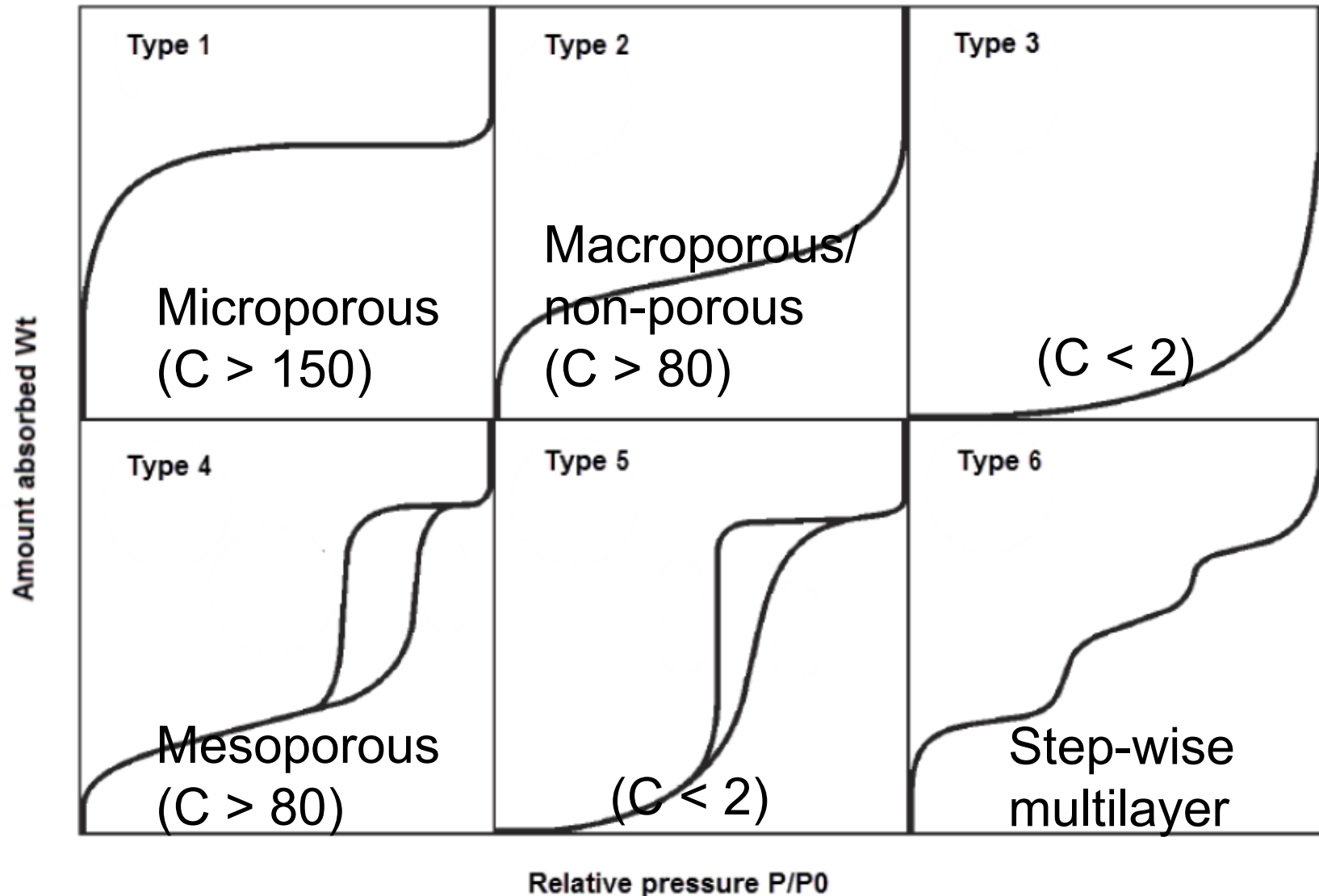
# Can only assume linear relationship for adsorption isotherms in the range of $0.05 < p/p_0 < 0.30$



# Pore width can make a big difference on shape of isotherm



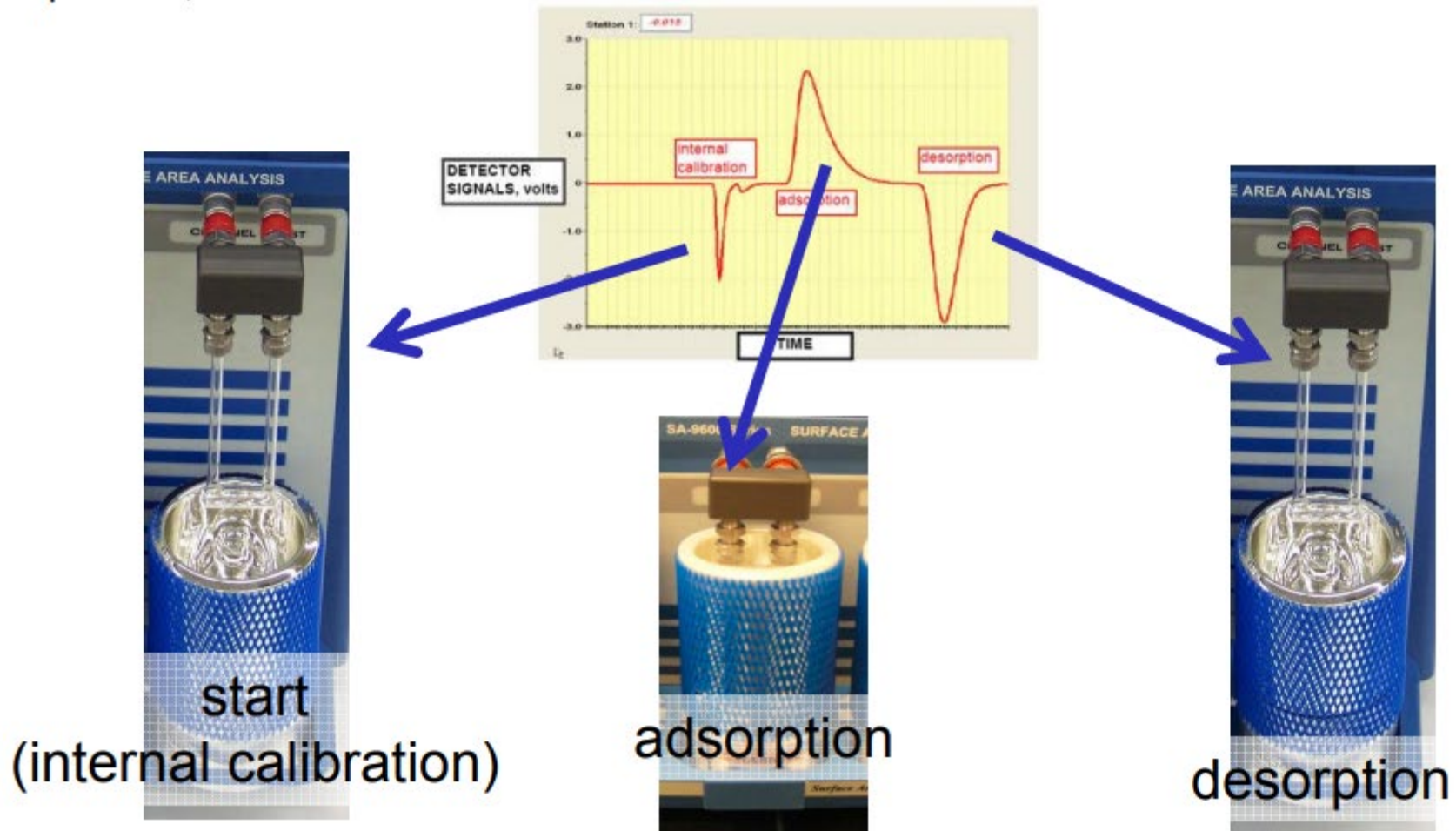
# Usually apply BET theory to Type 2 and Type 4 isotherms, apply to Type 1 with caution



# Have to insert sample into cell and degas sample to remove excess moisture on surface

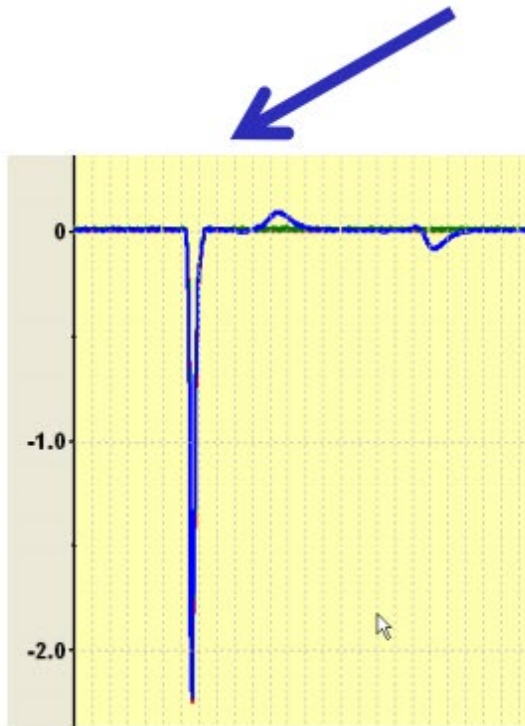


# BET measurement includes calibration of 1 cm<sup>3</sup> of nitrogen, adsorption, and desorption

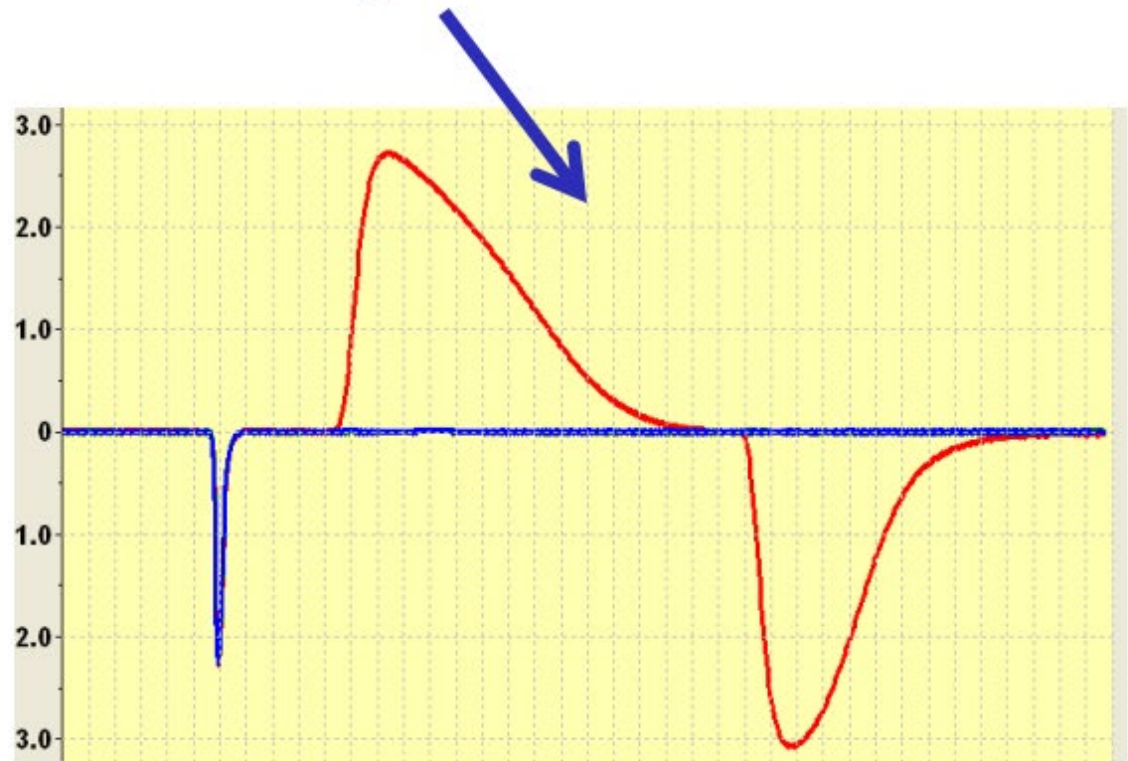


# Large surface area samples will adsorb and desorb more nitrogen

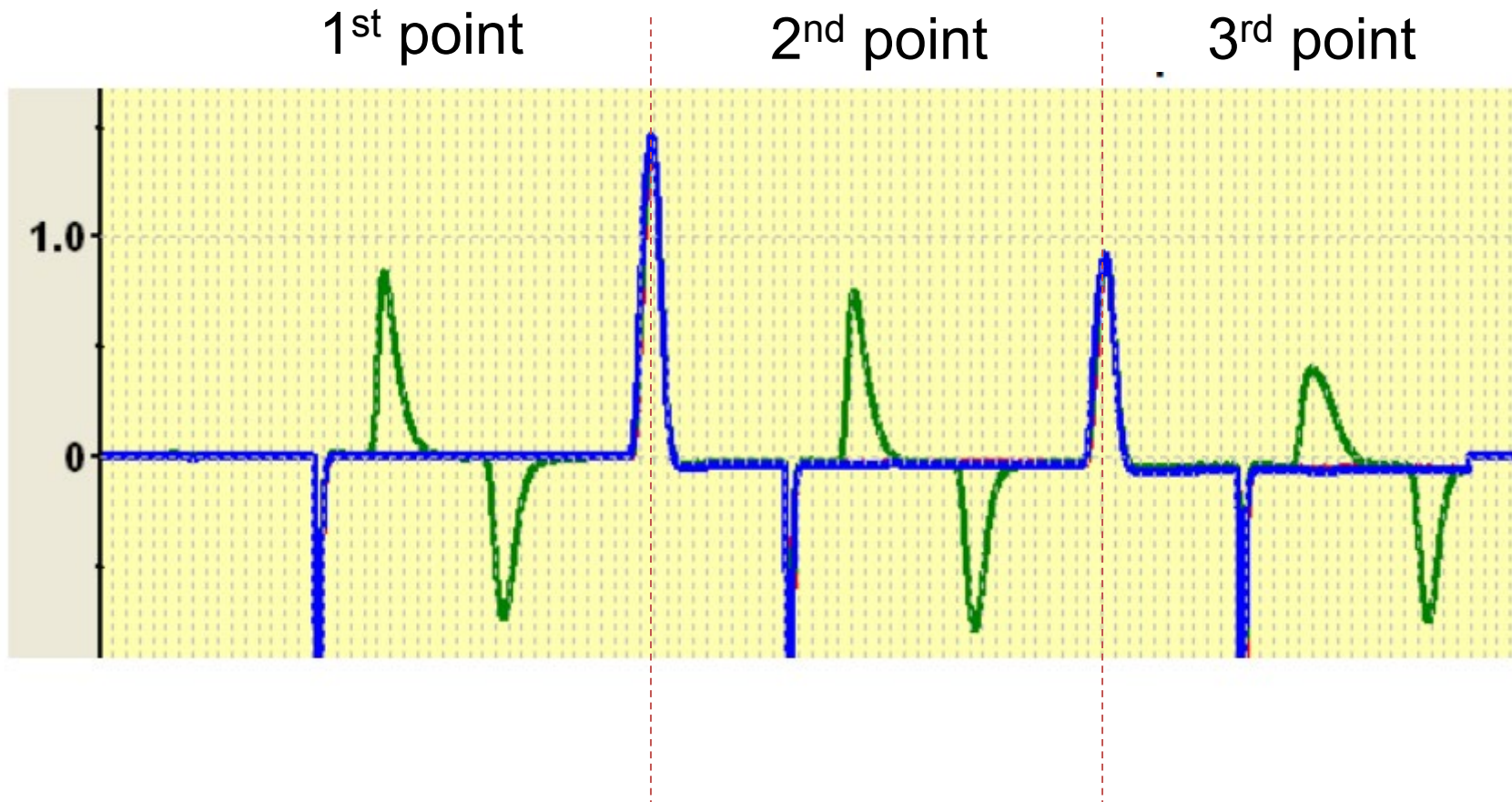
Small surface area



Large surface area



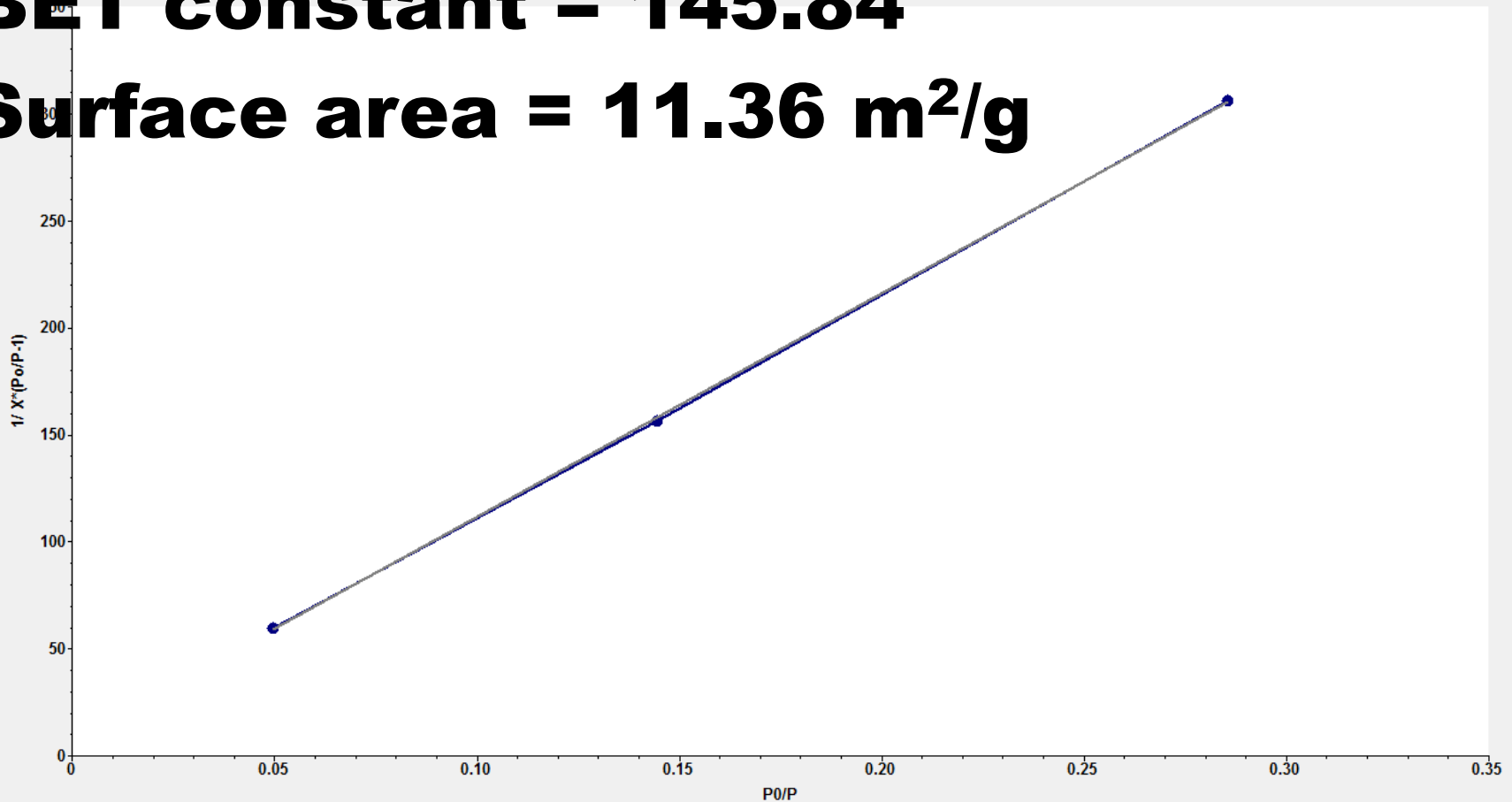
# BET multipoint measurement example



**Plot at least 3 points to obtain multi-point plot, solve for BET constant (c) and  $V_m$  (monolayer volume)**

**BET constant = 145.84**

**Surface area = 11.36 m<sup>2</sup>/g**



Thank you very much for your attention.

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